

# Automatic Harm to Competition?

Pricing Algorithms and Coordination

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25 April 2018

- Imagine a **parallel universe** where **technological progress runs in reverse**.
- Companies go from selling vast ranges of products online across geographic markets that are continental in scope to...



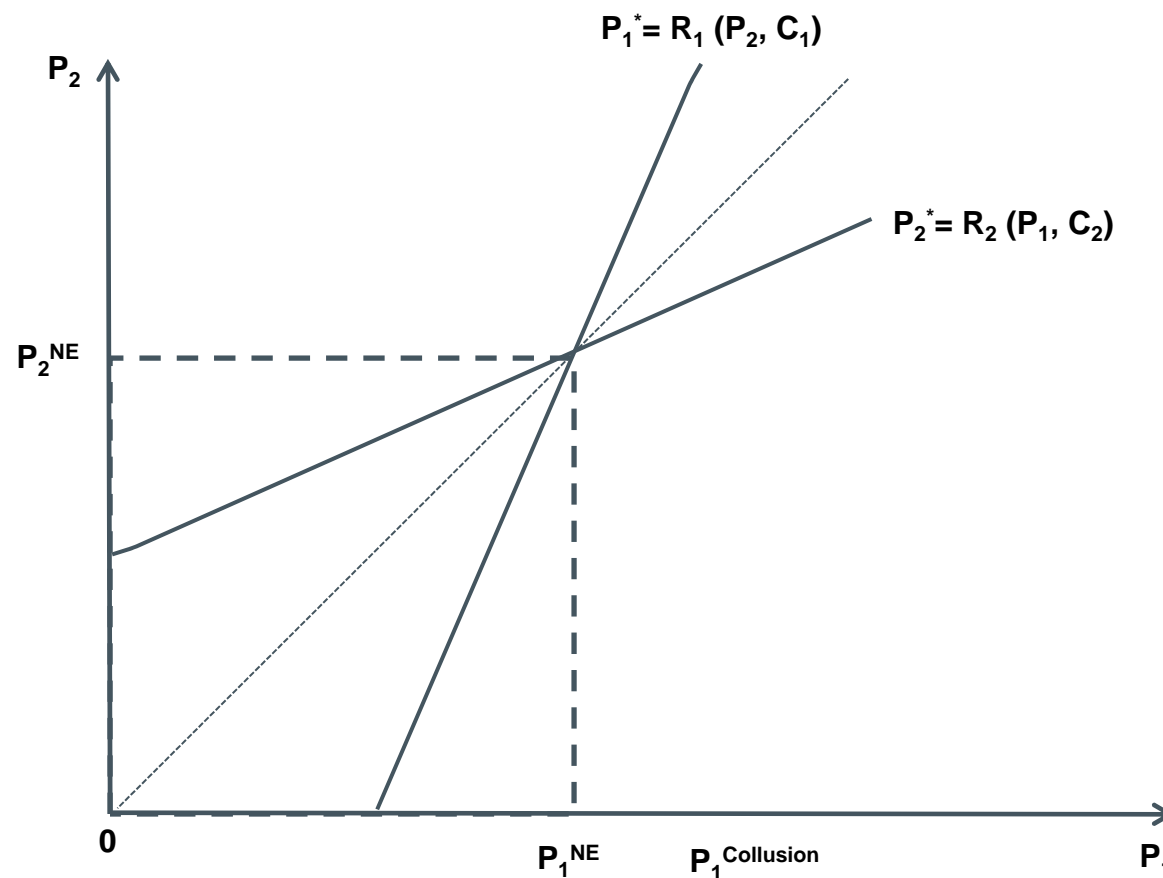
... selling single products in shops located in close proximity to one another.

The antitrust practitioners in this parallel universe are worried.

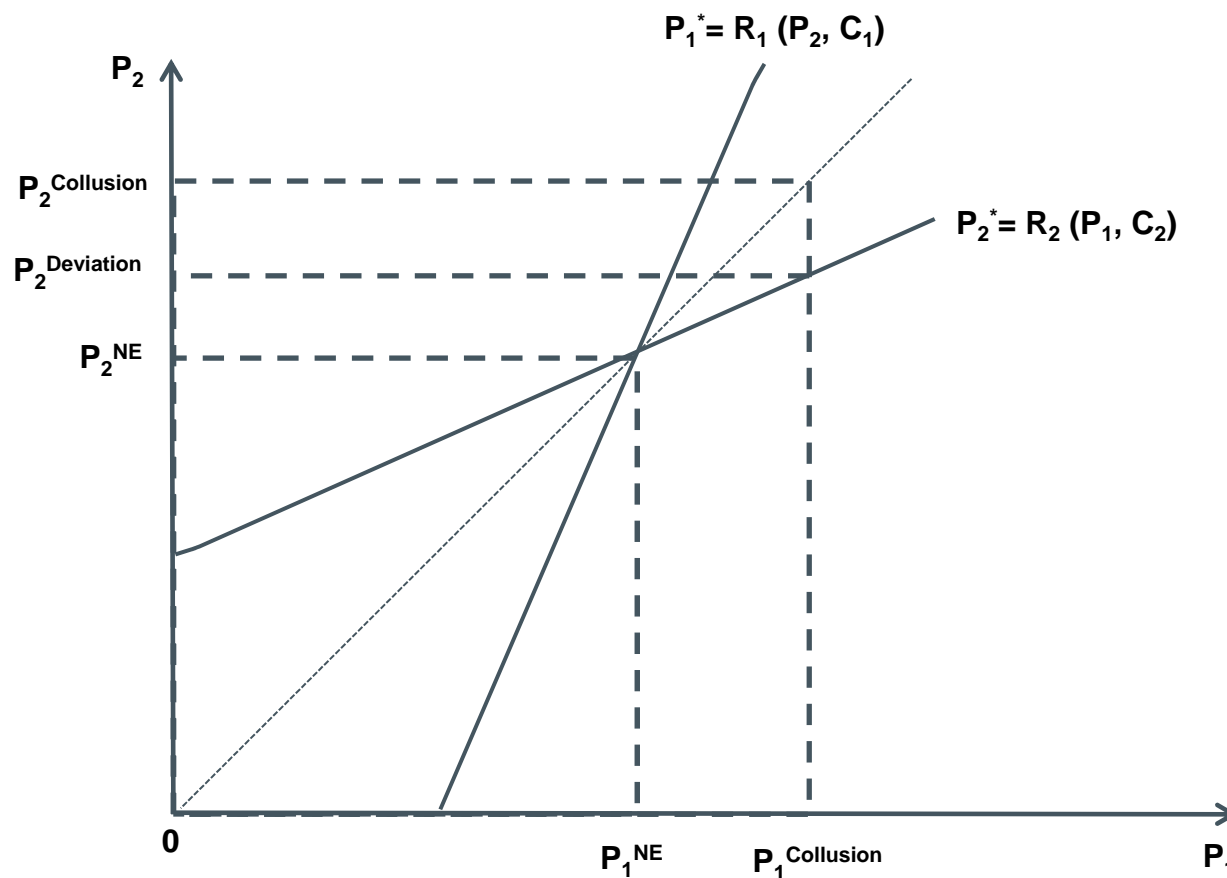
- Shouldn't we presume that tacit collusion will inevitably emerge in this setting?
- Do competition authorities have the tools to deal with the emerging risks of tacit coordination?

These are precisely the questions that arise with **algorithmic pricing**.

- Firms acknowledging their strategic interdependence when setting price **does not** imply tacit coordination



- A **defining** feature of tacit coordination is that individual firms can increase profits in the short run by taking some other action



- Collusion can be an equilibrium in a **repeated game** if PV of profits from deviating (and being punished) are lower than PV of profits from sticking to collusion
  - Simplest case – revert to one-shot Nash Equilibrium forever if observe deviation
- Deviation gives a higher payoff today and a lower payoff in all subsequent periods.
- Whether a firm prefers to deviate depends on its **patience** (measured by a discount factor).
- The **critical discount factor** is the discount factor that leaves a firm indifferent between colluding and deviating
- Economic theory's contribution to assessment of whether collusion is more or less "likely" to arise is insight into factors that affect critical discount factor - and therefore the **existence** of collusive equilibria.

- Factors that reduce the benefit from deviation, lower the critical discount factor
- Basic theoretical motivation for concerns with algorithmic pricing:
  - Algorithmic pricing → exploitation of **transparency** and **faster price reactions** → lower critical discount factor → bigger set of collusive equilibria
  - In a perfectly transparent market where firms interact repeatedly, when the **retaliation lag tends to zero**, collusion **can always be sustained** as an equilibrium strategy.

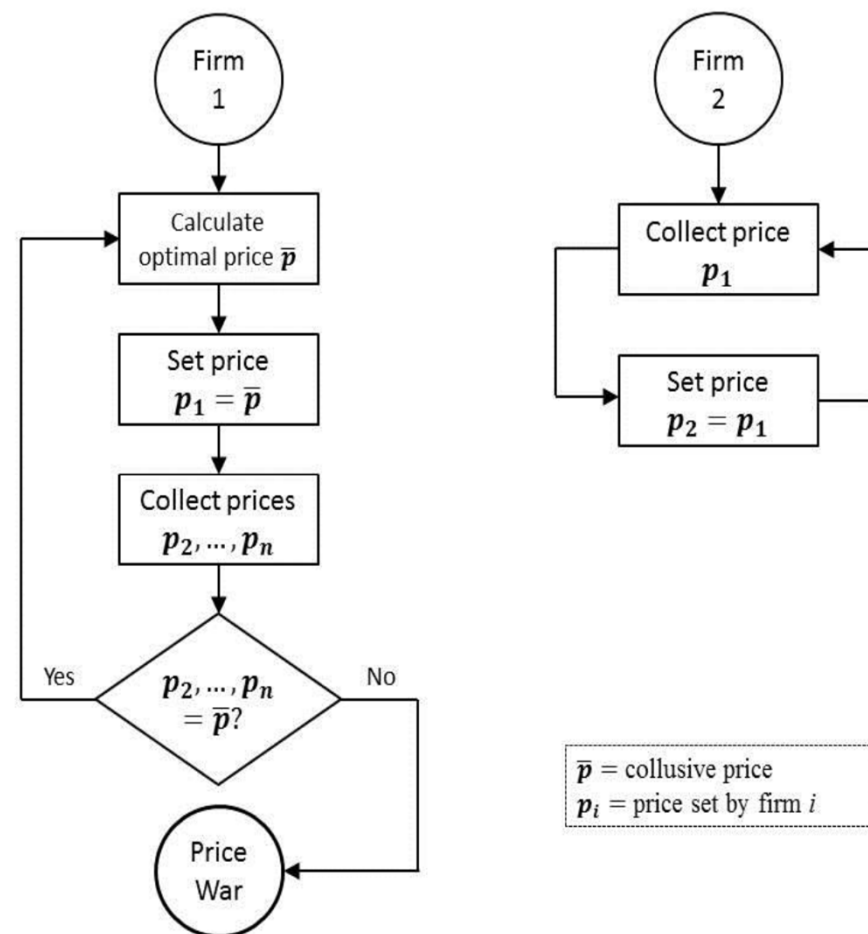


- Theory of repeated games is silent on how firms **reach** a collusive agreement (just about sustaining)
- Tacit coordination involves a problem of choosing amongst **multiple equilibria**
  - The NE of the one shot game repeated every period is always a (subgame perfect) NE of the super game **in addition** to any collusive equilibria
- This multiple equilibrium problem cannot be glossed over!

- Some commentators link strategic interdependence with the **inevitable emergence** of tacit coordination.
- Ezrachi and Stucke present an example of gas stations that can monitor and react to each other's prices and suggest that:
  - “*interdependence between gas station operators therefore supports a gradual increase in price and leads to a new equilibrium above competitive levels*”. Virtual Competition, Ezrachi and Stucke (2016)
- This is quite a leap from a theoretical perspective!

## Very simple algorithms?

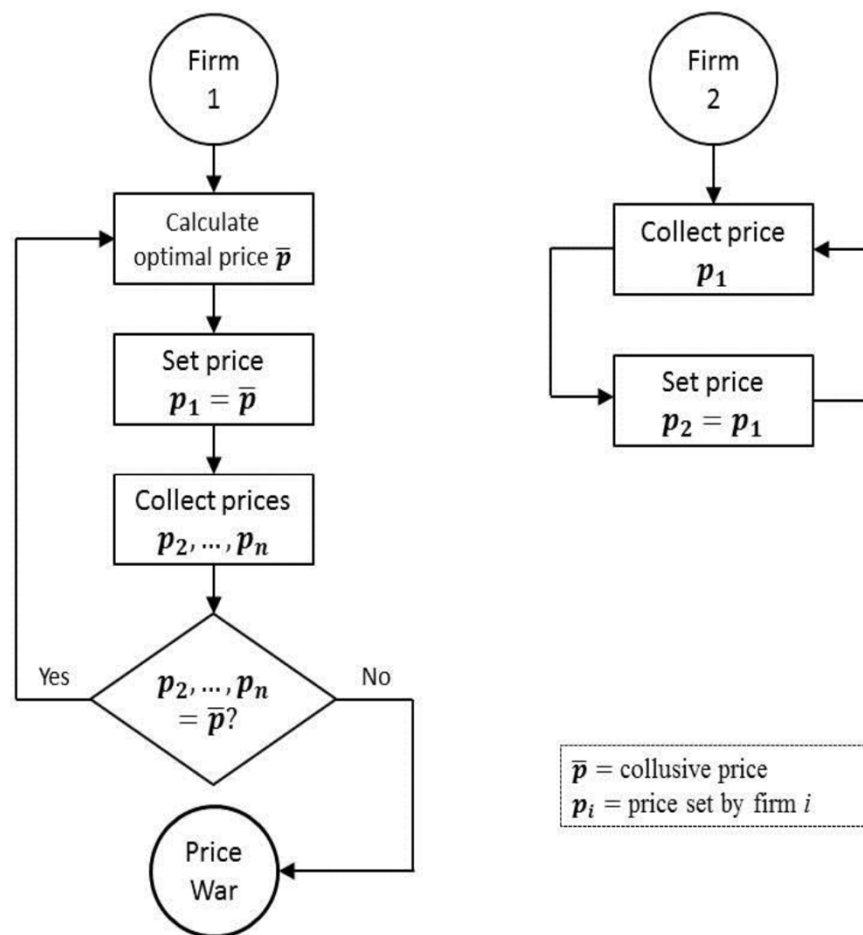
- E.g. OECD paper presents pair of simple **Leader-Follower algorithms**
  - Leader:
    - chooses optimal price
    - checks if follower chooses same price
    - If so, chooses new optimal price
    - If not, starts price war (forever?)
  - Follower:
    - chooses same price as leader.



Source: OECD

# What types of algorithms may cause concerns?

- But what if Follower:
  - “Tests” Leader by undercutting?
  - Makes a mistake?
- How does Leader react?
  - Committed to price war forever?
  - Forgive and forget?
- Need communication?
  - “The whole point of the doomsday machine is lost if you keep it a secret!” – Dr Strangelove



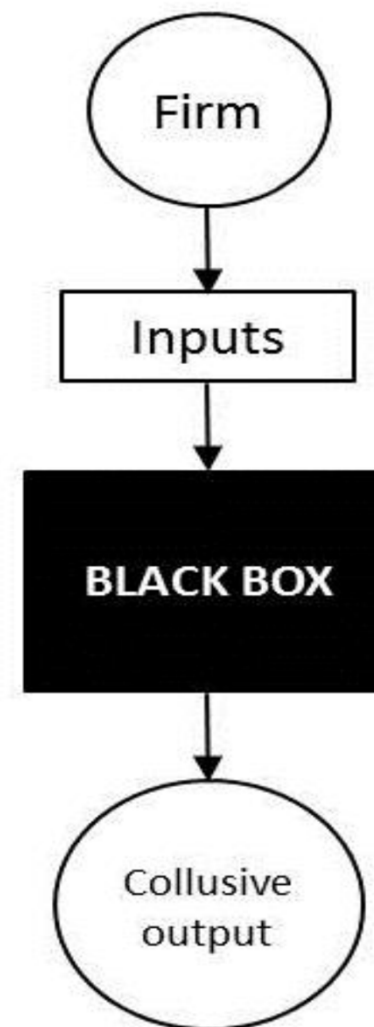
Source: OECD

# Simple strategies with BIG threats may prove costly (particularly when errors are possible)



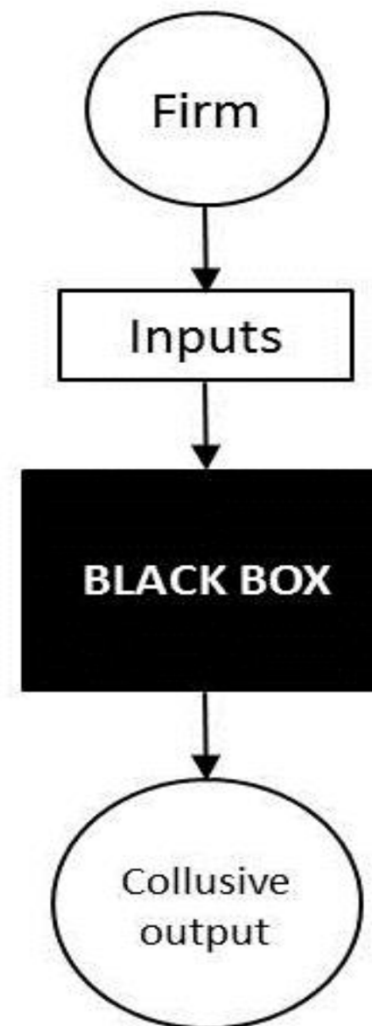
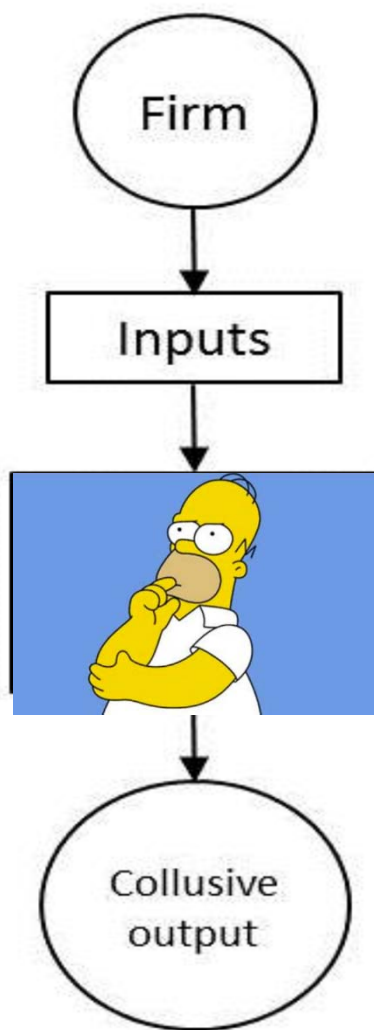
## Very complex algorithms?

- Risk that some algorithms with powerful predictive capacity, by constantly **learning and readapting to the actions of other market players** ...will be able to collude without the need for any human intervention (OECD).
- Likely that algorithms learning faster than humans are able through high-speed trial and error **to eventually reach** a cooperative equilibrium (OECD).



Source: OECD

# What types of algorithms may cause concerns?



Source: OECD

**Axelrod (1980)** ran an experiment that pitted many algorithms against one another playing a prisoner dilemma, e.g.

- **TIT FOR TAT**: Cooperate on first move, thereafter reciprocate opponent's previous action
- **JOSS**: Like TIT FOR TAT, but 10% of the time it defects if other player cooperated
- **FRIEDMAN**: Cooperative until the other player defects; then it never cooperates again

Some lessons:

- Algorithms that do not exhibit “forgiveness” (like FRIEDMAN) perform poorly.
- Even fairly forgiving algorithms can enter a death spiral due to “echo effects”, e.g. TIT FOR TAT vs. JOSS (see next slide)
- TIT FOR TAT won the tournament – but tournament would have been won by TIT FOR TWO TATS (defects only if other defected on last two moves) if it had been entered.
  - *“This should serve as a warning against the facile belief than an eye for an eye is necessarily the best strategy” - Axelrod*
- But TIT FOR TWO TATS performed poorly in a second tournament – where other algorithms were more aggressive!



*Axelrod / THE PRISONER'S DILEMMA 15*

TABLE 3  
Illustrative Game Between TIT FOR TAT and JOSS

moves	1- 20	11111	23232	32323	23232
moves	21- 40	32324	44444	44444	44444
moves	41- 60	44444	44444	44444	44444
moves	61- 80	44444	44444	44444	44444
moves	81-100	44444	44444	44444	44444
moves	101-120	44444	44444	44444	44444
moves	121-140	44444	44444	44444	44444
moves	141-160	44444	44444	44444	44444
moves	161-180	44444	44444	44444	44444
moves	181-200	44444	44444	44444	44444

Score in this game: TIT FOR TAT 236, JOSS 241

Legend: 1 both cooperated  
2 TIT FOR TAT only cooperated  
3 JOSS only cooperated  
4 neither cooperated

Salcedo (2015) – interesting paper that considers algorithms that *inevitably* collude

Assumptions about how the algorithms work:

1. **Commitment is feasible:** algorithms cannot be revised in the short-run; but also
2. **Commitment is imperfect:** algorithms can be revised over time
3. **Responsiveness:** algorithms rapidly react to market outcomes
4. **Observability:** rival's algorithm can be fully observed or (decoded)

**These are strong assumptions – so does this paper tell us we should be concerned?**

- Algorithms that facilitate personalised pricing may destabilise collusion
  - Massive increase in **complexity** of tacit agreements required!
  - Theoretical support for idea “allowing” price discrimination **hampers sustainability** of collusion - Helfrich and Herweg (2016)
- Algorithms that administer a platform may destabilise collusion
  - e.g. Amazon **Buy Box** (see next slide)
  - **~80%** of purchases on Amazon go through the Buy Box (Chen 2016).
  - Buy Box algorithm is not disclosed by Amazon (but understood to be based on a number of competitive variables, e.g. price, ratings, faster shipping options)
  - Amazon wants a competitive platform
  - Amazon may actively seek to undermine collusion by creating “**all or nothing**” competition for the Buy Box (e.g. via reducing rotation of Buy Box across sellers).

# Algorithms that administer a platform may destabilise collusion

Buy Box Price

Buy Box

The screenshot shows an Amazon product page for a red umbrella with a fireman theme. The product is titled "Fireman Sam Saving The Day Umbrella" by Fireman Sam. The price is \$12.99 plus \$1.00 shipping. The product is sold by THETRAVELBAGSHOP. There are handwritten annotations in orange: "Buy Box Price" with an arrow pointing to the price, "Buy Box" with an arrow pointing to the "Add to Cart" button, "New & Used" with an arrow pointing to the "3 new from \$12.99" text, and "Other Sellers" with an arrow pointing to the "Other Sellers on Amazon" section which shows a price of \$13.74 plus \$5.83 shipping.

amazon  
Your Amazon.com Today's Deals Gift Cards Sell Help  
Sponsored By Hershey's  
9 DAYS LEFT Halloween Shop >Shop now  
Shop by Department Search All fireman sam umbrella Go Hello, Sign in Your Account Try Prime Cart Wish List  
Patio, Lawn & Garden Best Sellers Deals Outdoor Décor Gardening Grilling Patio Furniture Landscaping Tools Pools & Spa Supplies Generators Snow Removal  
Clothing, Shoes & Jewelry Luggage & Travel Gear Umbrellas  
Fireman Sam Saving The Day Umbrella  
by Fireman Sam  
★★★★★ 1 customer review  
List Price: \$49.99  
Price: \$12.99 + \$1.00 shipping  
You Save: \$7.00 (35%)  
In Stock.  
Sold by THETRAVELBAGSHOP.  
• 100% Official Licensed Product  
3 new from \$12.99  
Share  
Qty: 1  
\$12.99 + \$1.00 shipping  
In Stock. Sold by THETRAVELBAGSHOP  
Add to Cart  
Turn on 1-Click ordering  
Add to Wish List  
Other Sellers on Amazon  
\$13.74 + \$5.83 shipping  
Sold by: Mrtoybox (UK goods)  
2 new from \$12.99

## When algorithms are used to implement an explicit agreement

- Traditional antitrust rules apply
- *“Companies can’t escape responsibility by hiding behind a computer program” - Vestager*

## When we have no evidence of explicit collusion

- Limited theoretical and empirical support for extending enforcement tools at this stage
- Stick to the “guy named Bob” test (Ohlhausen speech)
  - *“Is it ok for a guy named Bob to collect confidential price strategy information from all the participants in a market, and then tell everybody how they should price? If it isn’t ok for a guy named Bob to do it, then it probably isn’t ok for an algorithm to do it either.”*
  - Is it ok for guys named Bob to “adapt themselves intelligently to the existing and anticipated conduct of their competitors”? (Case 40/73 Suiker Unie EU:C:1975:174, para. 174) - **YES!**

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